Supplemental Materials: Contrasting Transport Performance of Electron- and Hole-Doped Epitaxial Graphene for Quantum Resistance Metrology

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Text I: Fittings of the low-field magnetoconductivity data

The low field magnetoconductivity curves for n- and p-type devices were fitted using the following formula that is widely used to describe the weak localization effect in graphene, ^[1]

$$\Delta\sigma(B) = \frac{e^2}{\pi h} \left[F(\frac{B}{B_{\phi}}) - F(\frac{B}{B_{\phi} + 2B_i}) - 2F(\frac{B}{B_{\phi} + B_i + B_*}) \right]$$
(S1)

where $F(z) = \ln z + \psi(1/2 + 1/z)$, $\psi(x)$ is the digamma function, $B_{\phi,i,*} = \hbar/(4De)\tau_{\phi,i,*}^{-1}$, *D* is the diffusion coefficient, and the characteristic scattering lengths are defined by $L_{\phi,i,*} = (D\tau_{\phi,i,*})^{1/2}$. As demonstrated in Fig. 3 and Fig. S4, all the data can be well fitted, and the values of L_{ϕ} can be extracted accordingly.

Text II: Estimation of the localization length

Fig. S5 further plots the conductance at 6 T as a function of temperature for two typical SiC/graphene devices (see Fig. 4 in the main text). It is clear that both the devices obey a well-defined variable range hopping (VRH) behavior of graphene, since the data can be well fitted via $\sigma_{xx} \propto \exp(-A/T^{1/2})$, where $A = (4\hbar v_F/k_B\xi)^{1/2}$, v_F is Fermi velocity, k_B is the Boltzmann constant, ξ is localization length.^[2] The extracted ξ for the n- and p-type devices are 30 nm and 97 nm, respectively.



Figure S1: Basic characterizations of SiC/graphene samples. (a) Typical atomic force microscopy image of a SiC/graphene sample, from which clear terrace morphology is seen. (b) Raman spectrum of a SiC/graphene sample. The full width at half maximum of the 2D peak is approximately 36 cm⁻¹, indicating that the graphene is primarily composed of a single layer.^[3,4] Inset: enlarged view of the 2D peak with a single Lorentzian fitting.



Figure S2: Raw data of the magneto-transport measurements at 5 K for various devices. [(a), (b)] Magnetic field dependence of (a) Hall resistivity ρ_{xy} and (b) longitudinal resistivity ρ_{xx} for n-type devices with different carrier densities. [(c), (d)] Magnetic field dependence of (c) ρ_{xy} and (d) ρ_{xx} for p-type devices.



Figure S3: Raw data of the magneto-transport measurements conducted at different temperatures. [(a), (b)] Magnetic field dependence of (a) ρ_{xy} and (b) ρ_{xx} for a n-type device at various temperatures. [(c), (d)] Magnetic field dependence of (c) ρ_{xy} and (d) ρ_{xx} for a p-type device with similar carrier density.



Figure S4: Fittings of the low-field magnetoconductivity data at various temperatures. [(a), (b)] Low-field magnetoconductivity data for (a) a n-type device and (b) a p-type one with similar carrier density. Here, $\Delta\sigma(B) = \sigma(B) - \sigma(0)$ corresponds to the change in conductivity relative to the zero-field value. The solid lines are fitting results using formula (S1). (c) The extracted values of phase coherence length at different temperatures for these two devices.



Figure S5: Estimation of the localization length based on the VRH mechanism. Conductance σ_{xx} vs $T^{-1/2}$ for the n- and p-type devices under a 6 T magnetic field, and the corresponding fitting results (black dashed lines).

References

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