## Supplemental Material: In-plane anisotropic response to the uniaxial pressure in the hidden order state of URu<sub>2</sub>Si<sub>2</sub>

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FIG. S1. (a)-(d) Temperature dependence of resistance for x = 0.2 and 0 along the (100) and (110) directions. The solid lines are fitted results by Eq. (1). (e)-(h) Temperature dependence of  $\zeta$  for x = 0.2 and 0 along the (100) and (110) directions. The solid lines are calculated results by Eq. (2).

## I. CALCULATING THE ELASTORESISTIVITY BASED ON THE GAP FUNC-TIONS

In the manuscript, we have shown that the temperature dependence of the elastoresistivity  $\zeta$  above  $T_0$  in the URu<sub>2-x</sub>Fe<sub>x</sub>Si<sub>2</sub> system can be simply explained as the uniaxial-pressure effect on an energy scale, which is most likely  $T^*$ . This scenario can be also applied below  $T_0$  except for the x = 0 sample along the (110) direction. Since the temperature dependence of the resistivity has long been known to be described by some gap functions [1, 2], the energy scale should be associated with the gap. Here we take a simple form as follows [1],

$$\rho = \rho_0 + AT^2 + \frac{BT}{\Delta} \left(1 + \frac{2T}{\Delta}\right) e^{-\frac{\Delta}{T}},\tag{1}$$

where  $\Delta$  is the gap associated with the HO transition. It is reasonable to assume that the application of pressure changes  $\Delta$  as  $\Delta \approx \Delta_0 + \kappa p$  when the pressure is small. Therefore, the resistivity change under pressure is proportional to  $d\rho/d\Delta$ , which is

$$\frac{d\rho}{d\Delta} = -\frac{B}{\Delta} \left(1 + \frac{3T}{\Delta} + \frac{4T^2}{\Delta^2}\right) e^{-\frac{\Delta}{T}}.$$
(2)

We can thus fit the temperature dependence of the resistance below  $T_0$  with Eq. (1) [Fig. S1(a)-S1(d)] and calculate  $dR/d\Delta$  according to Eq. (2). It is clear that the calculated

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results match the measured  $\zeta$  well for all the samples except the x = 0 sample along the (110) direction.



FIG. S2. Comparison between  $-\zeta$  and dR/dT for (a) x = 0.2 and p // (100), (b) x = 0.2 and p // (110), (c) x = 0 and p // (100), and (d) x = 0 and p // (110).

## II. COMPARISON BETWEEN $\zeta$ AND dR/dT

We have pointed it out in the manuscript that the temperature dependence of  $\zeta$  and dR/dT are very similar. Fig. S2 shows the comparison between  $-\zeta$  and dR/dT for all the samples. Again, all of them match well expect for the x = 0 sample along the (110) direction below  $T_0$ .

<sup>[2]</sup> S. Ran, C. T. Wolowiec, I. Jeon, N. Pouse, N. Kanchanavatee, B. D. White, K. Huang, D. Martien, T. DaPron, D. Snow, M. Williamsen, S. Spagna, P. S. Riseborough, and M. B. Maple, Phase diagram and thermal expansion measurements on the system URu<sub>2-x</sub>Fe<sub>x</sub>Si<sub>2</sub>, Proc. Natl. Acad. Sci. U.S.A **113**, 13348 (2016).