# Supporting Information for "Anisotropic Magnon-Magnon Coupling in Synthetic Antiferromagnets"

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# 1. The description of the energy model

For the case when the external magnetic field H is applied in the plane of films, the energy for the system including two identical ferromagnetic layers is[1]

$$E = \sum_{i=1}^{2} d_{i} \left[ -M_{i} H \cos(\theta_{i} - \theta_{H}) - K_{u} \cos^{2} \theta_{i} \right] + J_{1} \frac{M_{1} \cdot M_{2}}{M_{1} M_{2}} + J_{2} \left( \frac{M_{1} \cdot M_{2}}{M_{1} M_{2}} \right)^{2}.$$

where  $M_1 = M_2 = M_s$  is the magnetization for each CoFeB layer, and  $d_i$  (*i*=1,2) is the

thickness for the top and bottom layer, i.e.,  $d_1$  is 12 nm and  $d_2$  is 10 nm.  $K_u$  is the uniaxial in-plane anisotropy. Its easy axis is defined as the x-axis.  $\theta_i$  and  $\theta_H$  are defined as the angle of equilibrium directions for two magnetizations and the external field with respect to the x-axis, respectively. Here, both the so-called bilinear coupling constant  $J_1$ and biquadratic coupling constant  $J_2$  are included. The equilibrium configuration ( $\theta_1$  and  $\theta_2$ ) can be obtained through find the minimum of energy. At zero field, if  $J_1$  is positive, the bilinear coupling favors two magnetic layers antiparallel. It is the so-called antiferromagnetic coupling. On other hand,  $J_2$  is positive, the biquadratic coupling favors the two magnetizations 90°-type coupling. More cases have been discussed in ref.[2].

#### 2. The solution of ferromagnetic resonance in SAF

For convenience, we define an effective anisotropy field and effective exchange fields as  $H_u=2K_u/M$ ,  $H_{ex1}^{(i)} = \frac{J_{1,i}}{Md_i}$ , and  $H_{ex2}^{(i)} = J_{2,i}/Md_i$ , *i*=1,2 for the top and bottom magnetic layer, respectively. Based on the coupled Landau-Lifshitz equation (LL), the resonance frequency of magnetization precession can be treated as the solution of the linearized LL equation in the case of a small amplitude of magnetization precession. The dispersion is numerical determined as the eigenvalue of the following matrix:[1]

$$\begin{bmatrix} 0 & H_1 & 0 & H_2 \\ -H_3 & 0 & H_4 & 0 \\ 0 & H_6 & 0 & H_5 \\ H_8 & 0 & -H_7 & 0 \end{bmatrix},$$

where

$$\begin{split} H_{1} &= H \cos \overline{\mathbb{H}}_{0} - \theta_{H} + H_{u} \cos \overline{\mathbb{H}}_{2} (\theta_{1} - \theta_{u}) + 4\pi M_{s} + H_{ex1}^{(1)} \cos \overline{\mathbb{H}}_{0} - \theta_{2}) \\ &- 2H_{ex2}^{(1)} \cos \overline{\mathbb{H}}_{2} (\theta_{1} - \theta_{2}) \\ H_{2} &= -H_{ex1}^{(2)} + 2H_{ex2}^{(2)} \cos(\theta_{1} - \theta_{2}) \\ H_{3} &= H \cos(\theta_{1} - \theta_{H}) + H_{u} \cos[2(\theta_{1} - \theta_{u})] + H_{ex1}^{(1)} \cos(\theta_{1} - \theta_{2}) \\ &- 2H_{ex2}^{(1)} \cos[2(\theta_{1} - \theta_{2})] \\ H_{4} &= H_{ex1}^{(2)} \cos(\theta_{1} - \theta_{2}) - 2H_{ex2}^{(2)} \cos[2(\theta_{1} - \theta_{2})] \\ H_{5} &= H \cos(\theta_{2} - \theta_{H}) + H_{u} \cos \overline{\mathbb{H}}_{2} (\theta_{2} - \theta_{u})] + 4\pi M_{s} + H_{ex1}^{(2)} \cos(\theta_{1} - \theta_{2}) \\ &- 2H_{ex2}^{(2)} \cos \overline{\mathbb{H}}_{2} (\theta_{1} - \theta_{2})] \\ H_{6} &= -H_{ex1}^{(1)} + 2H_{ex2}^{(1)} \cos(\theta_{1} - \theta_{2}) \\ H_{7} &= H \cos(\theta_{2} - \theta_{H}) + H_{u} \cos[2(\theta_{2} - \theta_{u})] + H_{ex1}^{(2)} \cos(\theta_{1} - \theta_{2}) \\ &- 2H_{ex1}^{(2)} \cos[2(\theta_{1} - \theta_{2})] \\ H_{8} &= H_{ex1}^{(1)} \cos(\theta_{1} - \theta_{2}) - 2H_{ex2}^{(1)} \cos[2(\theta_{1} - \theta_{2})] \end{split}$$

The eigenvalue is  $-i\omega/\gamma = -i2\pi f_r/\gamma$ .

# 3. The FMR spectra for $t_{\rm Ir}$ =1.2 nm at varying $\theta_{\rm H}$

The ferromagnetic resonance spectra were acquired at varying the magnetic field direction  $\theta_{\rm H}$ . Since the anisotropy of the gap is larger in the sample with  $t_{\rm Ir} = 1.2$  nm, the spectra for  $t_{\rm Ir} = 1.2$  nm is presented in Fig. S1. The red circle curves are calculated based on the parameters from Table I and are also plotted in Fig. S1. At low angles like  $\theta_{\rm H} = 18^{\circ}$  and  $30^{\circ}$  (see Fig. S1(a) and (b)), the location of the anticrossing gap closes to the spin-flop field. After spin-flop, the magnetization is not aligned uniformly immediately but after a field window since the broaden distribution of IEC and  $H_{\rm u}$ . It brings the

disturbance for counted the gap. Therefore, a significant deviation happens due to this

non-uniform.

### REFERENCES

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- [2] Demokritov S O 1998 Biquadratic interlayer coupling in layered magnetic systems *J. Phys. D: Appl. Phys.* **31** 925–41



Fig. S1. FMR spectra for CoFeB(10 nm)/Ir(1.2 nm)/CoFeB(13 nm) at varying  $\theta_{H}$ , (a)

 $\theta_{H}=18^{\circ}$ , (b),  $\theta_{H}=30^{\circ}$ , (c)  $\theta_{H}=45^{\circ}$ , (b),  $\theta_{H}=70^{\circ}$ , respectively. The red circle curves are

calculated based on the parameters from Table I.



Fig. S2. The illustration of VNA-FMR setup. The sample is rotated in in-plane.  $\theta_H$  is the angle between its easy axis and the external field.