## **Supplementary Information:**

## Novel Superconducting Electrides in Ca–S System under High Pressures

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## **Computational Details**

We have explored the pressure-induced structural evolution in Ca–S system with various  $Ca_mS_n$  (m = n = 1-4) using the CALYPSO and USPEX codes with simulation cell sizes of 1-4 formula units (f.u.) at temperature of 0 K and pressures at 0, 50, 100, 150 and 200 GPa. Such methods have been successfully employed in various systems. The CALYPSO structure searching: In the first step, random structures with certain symmetry are constructed in which atomic coordinates are generated by the crystallographic symmetry operations. After processing the first generation structures, 60% of them with lower Gibbs free energies are selected to construct the next generation structures by PSO (Particle Swarm Optimization). 40% of the structures in the new generation are randomly generated. A structure fingerprinting technique of bond characterization matrix is applied to the generated structures, so that identical structures are strictly forbidden. The energy convergence was set to 10-5 eV. The USPEX structure searching: In the evolutionary structural searching, the first generation of structures was always created randomly with its population size of 20-60 structures. The succeeding generations are produced by variation operator heredity (60%), lattice mutation (30%) and permutation (10%).



Figure S1. Calculated formation enthalpies of various Ca–S compounds at 0 GPa.



**Figure S2.** The calculated phonon spectra of the predicted stable Ca-rich compounds at selected pressures. (a)  $P2_1/m$  Ca<sub>3</sub>S at 60 GPa (b) P4/mbm Ca<sub>3</sub>S at 150 GPa (c) Pnma Ca<sub>2</sub>S at 50 GPa (d) Cmcm Ca<sub>2</sub>S at 150 GPa (e) Fm-3m CaS at 0 GPa (f) Pm-3m CaS at 100 GPa (g)  $I4_1/amd$  CaS at 200 GPa.



**Figure S3.** The calculated phonon spectra of the predicted stable S-rich compounds at selected pressures. (a) *Fddd* CaS<sub>2</sub> at 150 GPa (b) *P*-42<sub>1</sub>*m* CaS<sub>3</sub> at 100 GPa (c) *Immm* CaS<sub>3</sub> at 200 GPa (d) C2/c CaS<sub>4</sub> at 200 GPa.



**Figure S4.** The calculated electron localization function (ELF) for  $CaS_2$  and  $CaS_4$ . (a) *Fddd*  $CaS_2$  (b) C2/c  $CaS_4$  and (c) projected density of states (PDOS) for  $CaS_2$  and  $CaS_4$ .



**Figure S5.** The calculated electron localization function (ELF) for  $CaS_3$ . (a) *P*-42<sub>1</sub>*m* (b) *Immm* and (c) projected density of states (PDOS) for  $CaS_3$ .



**Figure S6.** The calculated electron localization function (ELF). (a) *P4/mbm* Ca<sub>3</sub>S (b) *Cmcm* Ca<sub>2</sub>S and (c) projected density of states (PDOS) of *P4/mbm* Ca<sub>3</sub>S, *Pnma* Ca<sub>2</sub>S and *Cmcm* Ca<sub>2</sub>S.



**Figure S7.** The calculated electron localization function (ELF) for CaS. (a) Fm-3m (b) Pm-3m (c)  $I4_1/amd$  and (d) projected density of states (PDOS) for CaS.

Space group	Lattice parameters	Atomic coordinates (functional)	Sites
pressure	(Å, )	Atomic coordinates (fractional)	Sites
<i>P2</i> <sub>1</sub> / <i>m</i> Ca <sub>3</sub> S 50 GPa	a=11.7601 b=3.9581 c=5.2798 $\alpha = \gamma = 90$ $\beta = 95.413$	Ca10.717460.750000.43627Ca20.818560.250000.25522Ca30.461730.750000.31037Ca40.360820.250000.06974Ca50.111970.250000.11684Ca60.017560.750000.32048S10.239800.750000.25497S20.590000.250000.21484	2e 2e 2e 2e 2e 2e 2e 2e
P4/mbm Ca <sub>3</sub> S	a=b=4.8148	Ca1 0.30036 -0.80036 0.00000	4g
200 GPa	c=3.2719	Ca3 0.00000 -0.50000 -1.50000	2c
	$\alpha = \beta = \gamma = 90$	S1 0.50000 -0.50000 -1.50000	2b
Pnma Ca <sub>2</sub> S	a=4.9357	Ca1 0.80971 0.25000 0.55808	4c
100 GPa	b=3.7499	Ca3 0.79889 0.25000 0.87482	4c
	c=7.8553	S1 1.10750 0.75000 0.80442	4c
	α=β=γ=90		
Cmcm Ca <sub>2</sub> S	a=2.7546	Ca1 0.50000 0.22561 0.75000	4c
200 GPa	b=10.6536	Ca2 0.50000 0.42441 1.25000	4c
	c=3.8931	S1 -0.00000 0.40158 0.75000	4c
	$\alpha = \beta = \gamma = 90$		
Fm-3m CaS	a=b=c=5.7101	Ca1 0.50000 0.50000 1.00000	4a
0 GPa	α=β=γ=90	S1 0.50000 0.50000 0.50000	4b
Fm-3m CaS	a=b=c=2.90180	Ca1 -1.50000 -1.50000 -0.50000	1b
100GPa	α=β=γ=90	S1 -1.00000 -1.00000 -1.00000	1a
I41/amd CaS	a=b=3.3034	Ca1 -1.00000 1.50000 0.25000	4a
200 GPa	c=7.0815 $\alpha=\beta=\gamma=90$	S1 -1.50000 0.50000 0.00000	4b
$\frac{Fddd}{200} \text{GPa}$	$a=7.4559b=4.3278c=6.8838\alpha=\beta=\gamma=90$	Ca1 0.75000 0.75000 0.25000 S1 0.25000 0.75000 0.10063	8a 16g
$P-42_1m$ CaS <sub>3</sub>	a=b=5.4158	Ca1 0.00000 -0.00000 -0.50000	2b
100 GPa	c=3.0567	S1 0.50000 -0.00000 -0.41780	2c
	α=β=γ=90	S3 0.20088 0.70088 -0.99872	4e
Immm CaS <sub>3</sub>	a=6.7265	Ca1 -0.50000 -0.50000 -0.50000	2a
200 GPa	b=3.8997	S1 -0.21893 -0.50000 -0.00000	4f
	c=2.734	\$9 -0.50000 -1.00000 -0.00000	2b
	$\alpha = \beta = \gamma = 90$		
<i>C</i> 2/ <i>c</i> CaS <sub>4</sub> 200 GPa	a=7.97428 b=2.86929 c=11.95417 $\alpha = \gamma = 90$	Ca1 0.00000 0.49966 0.75000 Ca2 0.50000 0.99966 0.75000 Ca3 0.00000 0.50034 0.25000 Ca4 0.50000 0.00034 0.25000 S1 0.88316 0.00020 0.33897	1a 1a 1a 1a 1a
	β=139.9	S2 0.66275 0.00030 0.01903	1a
		S3 0.38316 0.50020 0.33897	1a

**Table S1** Structural parameters of Ca-S system at selected pressure.

	S4 0 16275	0 50030	0.01903	1a
	S5 0 11684	0.00020	0.16103	1a
	S6 0 33725	0.00020	0.48097	1a
	S7 0 61684	0.50020	0.16103	1a
	S8 0 83725	0.50020	0.48097	19
	S9 0 11684	0.99980	0.46007	10
	S10.0 33725	0.99970	0.98097	10
	S11 0 61684	0.49980	0.66103	10
	S12 0 83725	0.49970	0.00105	10
	S12 0.03725	0.99980	0.93897	19
	S13 0.66275	0.99970	0.51903	10
	S15 0 38316	0.77770	0.83897	10
	S16 0 16275	0.49970	0.51903	10
	510 0.10275	0.47770	0.51705	14